

# **The New Weibull Handbook**

**Reliability & Statistical Analysis for Predicting Life, Safety,  
Risk, Support Costs, Failures, and Forecasting Warranty  
Claims, Substantiation and Accelerated Testing,  
Using Weibull, Log Normal, Crow-AMSAA ,  
Probit, and Kaplan-Meier Models**

**Fifth Edition by Dr. Robert B. Abernethy  
Author and Publisher**

## **The New Weibull Handbook, Fifth Edition**

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## ***Dedication:***

This book is dedicated to my wife, Sally, for her encouragement and patience. Further, it is dedicated to all my friends and colleagues that helped so much. Finally, it is dedicated to the reader with the hope it will have "some utility," to use Professor Weibull's words.

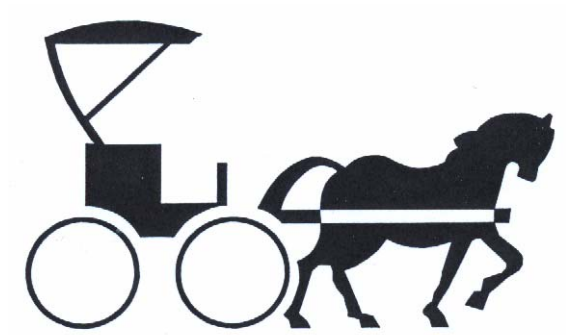
And lastly we have a special note for the Weibull Workshop students for whom we designed this Handbook...

### ***Weibull Workshop Students:***

If you are fortunate enough to have obtained or borrowed the Handbook before your Workshop, studying the Handbook before the Workshop is very helpful. **Please** read at least Chapters 1-4. We will cover the basic standard method the first day, Chapters 1-4. For the second day, study Chapters 5-7 (7 is least important). For the third day, Chapters 8, 9, & 10. (Most important material for the third day is the Crow-AMSAA Model.) Chapter 11 is case studies which you should browse. Please bring a clear plastic ruler, a calculator, and a problem from your work. The data should be in a single column, positive values are failures, negative are suspensions. You may bring the data in ASCII format, or a spreadsheet file (Excel) or WinSMITH Weibull files. The file may be on a diskette or in your laptop.

"Now in building of chaises, I tell you what,  
There is always *somewhere* a weakest spot,-  
In hub, tire, felloe, in spring or thill,  
In panel, or crossbar, or floor, or sill,  
In screw, bolt, throughbrace,-lurking still,  
Find it somewhere you must and will,-  
Above or below, or within or without,-  
And that's the reason, beyond a doubt,  
A chaise *breaks down*, but doesn't *wear out*.

Oliver Wendell Holmes... "The One-Hoss Shay"



# PREFACE

**Background** A quarter of a century has passed since the *USAF Weibull Analysis Handbook* was published. In the years that followed, the author frequently taught Weibull analysis using the USAF Handbook as the text, encouraged by both the United States Air Force and Pratt & Whitney. In 1987, the author retired early to devote full time to research and lecturing in Weibull Analysis. It has been most enjoyable and interesting. The best part has been meeting outstanding engineers from many industries with new and different applications for Weibull methods. The students inspire additional research and methods development. This in turn required rewriting and updating the USAF Handbook producing *The New Weibull Handbook*. This document is the fifth edition. It contains the latest methods, techniques, and applications that have been developed by the author, Wes Fulton, Paul Barringer, Joe Wauben, Bob Rock, Wayne Nelson, Randy Pirtle, Todd Marquart, Carl Tarum, Geoff Cole and David Navell and many others.

**The New Weibull Handbook** has become the national and international standard for Weibull analysis. It is in daily use throughout the world. Thousands of copies have been distributed. Users include military, automotive, medical, electronics, materials & composites research, aerospace, electrical power, nuclear power, dental research, advertising, bearings, compressors, v-belts, chain drives and on and on. Many organizations have adopted the Handbook and software implementing its methods as standard including the Federal Aviation Administration, Harley Davidson, Motorola, TVA, Honeywell, BICC General, GKN Automotive, Dupont, Meritor Automotive, Teleflex, Guidant Cardiac Pacemaker (CPI), Daimler Chrysler, General Electric, Siemens, Behr, Borg-Warner, NASA, Rolls Royce, Gates Rubber, the US Naval Air Arm (NAVAIR), the US Air Force at SAALC and WPAFB, and Dow Chemical. The author has provided many free copies (shipping charges only) of the Handbook to universities in Europe, North America, and Australia. The author hereby extends this offer to university libraries worldwide. Wes Fulton provides free demonstration copies of the SuperSMITH software on his web site.

With this fifth edition there is a new companion text, "The New Weibull Handbook Student Version." It includes an introductory version of the WinSMITH Weibull Software. The author provides free copies (shipping charges only) of the student handbook and the student software to professors and lecturers that teach reliability as well as to university libraries that request copies.

The **SuperSMITH** software is the most significant technical breakthrough. Wes Fulton has created friendly, easy-to-use software that does everything in the Handbook. *The New Weibull Handbook* provides an understanding and reference for SuperSMITH. The computer software has made application so much easier. It has also made teaching Weibull easier, more efficient, and more fun. Within the Weibull workshops, many more applications and case studies can be treated without the drudgery of hand calculations and plotting. As this document is the workbook for the Weibull Workshops, many references to the software capabilities are included. This referencing may appear to be inappropriate, but the reliance on software in the workshops requires it. If the student using *The New Weibull Handbook* desires, he may avoid almost all hand calculations and hand plotting by using SuperSMITH. The new "Playtime with SuperSMITH" computer tutorial enhances the Handbook and provides many step-by-step case studies illustrating all the methods. Alternatively, the reader may use this Handbook to write "home-grown" software. Outputs are easily validated with benchmark case studies found in both demonstration and full versions of the SuperSMITH software.

The **Fifth Edition** features new technology:

- Goodness of fit, illustrating for the first time the "power" of the three best methods for goodness of fit: Critical Correlation Coefficient, likelihood ratio and Anderson-Darling. "Power" is the probability that the method makes the correct choice identifying the parent distribution for a give data set.
- Crow-AMSAA modeling has become so popular that it has been moved to a new chapter. The new write-up includes the latest methods from the new IEC standards with best practices recommended.
- A new sections on warranty analysis has been added by Joe Wauben of Honda
- Life Cycle Costs are presented in a new section by Paul Barringer.
- Wayne Nelson has updated his on graphical repair analysis with a case study in Appendix M.

- Bob Rock of PACCAR updated his extremely useful life data analysis logic diagram which takes you step-by-step to the best methods and analysis for your particular data. The logic diagram is also available in Spanish.
- Todd Marquart of Micron Technology has completed an extensive comparison of the three methods for interval and grouped data. Which is most accurate?
- The New Weibull Handbook is unique in recommending “best practices” wherever there are alternative methods available. Some of the “best practices” have changed based on new research.
- Cost analysis is described for production process reliability, failure forecasts, Crow-AMSAA, Life Cycle Costs and optimal parts replacement.

To make the Handbook more readable, all the heavy mathematics will be found in the appendixes. Asterisks on section subtitles indicate advanced topics. The novice reader may skip these advanced sections. As the workbook is designed for the Weibull Analysis Workshops, the format includes much white space for notes and calculations. Dozens of case studies are employed to present the methodology. Paul Barringer has taken the most important reference texts and papers from my library and put them on his Website for downloading. <http://www.barringer1.com> They are indicated by a \$ sign preceding references throughout the Handbook..

**Thank You:** Many friends, students, experts, and clients have helped and contributed much to the Handbook. For me, all this support has been overwhelming. Everyone helped! Thank you all. Some are mentioned here:

- First, my associate, Wes Fulton, not only for his friendly software, but also for his research and development of new Weibull methods.
- Second, our associate, Paul Barringer, for his help, comments, reviews, research, and contributions.
- A board of industry experts has reviewed the fifth edition and provided many comments and contributions: Walter Thomas, Wes Fulton, Ronald Schop, Bob Rock, Charles DeSica, Randy Pirtle, Todd Marquart, Carl Tarum, Geoff Cole, Paul Barringer, Jim Breneman, and Joe Wauben. I am indebted to them.
- Many contributed sections of the Handbook: Bob Rock, PACCAR; David B. Smith, Detroit Edison; Bob Scanlon, Southern Pacific (now with the US Postal Service); Sten-Åke Irell, Volvo Flygmotor; Marie Stanton, FPL; David Weber, Consultant; Carl Tarum, Delphia; Hans Iwand, Union Pacific; Drs. Memis and Lautenschlager, Dentists at Northwestern University; Richard Rudy, Chrysler; Kenneth Young, Hydri; Jim Keener and Mel Thomas, FPL; Bill Pritchard, TVA; Shashank Kolhatkar, Borg Warner; Charlie Williams, Florida Power; Geoffrey Cole and David Navell, Rolls Royce; David Williamson, Dow Chemical; M.A. Vasan, Meritor Automotive; David B. Smith, Detroit Edison; and David Langanke and Randy Pirtle, Honeywell Engines.
- This edition is improved by incorporating the suggestions from the excellent constructive review of the Handbook by Dr. Alan Winterbottom for the Royal Statistical Society Journal A (1997), 160, Part 2. The author is indebted.
- None of the above are in any way responsible for errors in the Handbook. The author takes all the blame.

Please call or write with questions, comments, and constructive criticism about *The New Weibull Handbook*. I would like to hear from you: E-mail is preferred: [weibull@att.net](mailto:weibull@att.net)

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